Note: This lecture is best taken with Excel@ file LectureSIM.xls. Please pause the video and open Excel@ LectureSIM.xls, then continue. You may like to pause whenever you need to understand and repeat what is covered here.

## SIMULATION

The objectives of simulation:

1) To estimate the unknown population mean  $\mu_0$  (the average profit) with the confidence interval developed through the grant mean and the standard deviation of MonteCarlito,

$$\overline{x} \pm z \, s_{\overline{x}} \qquad \overline{p} \pm z \, \sqrt{p} (1 - \overline{p})/n$$

- 2) To estimate the unknown population proportion (of loss) with the confidence interval developed through the grant proportion of MonteCarlito
- 3) The value of z is given by =NORMSINV(1- $\alpha$ ), Z = 1.96 for 1- $\alpha$  = 0.95
- 4) Conclusions of simulation study:
  - a) We are 95% sure that the unknown true population mean (profit) is between the calculated lower and upper limits for the mean.
  - b) We are 95% sure that the unknown true population proportion (loss) is between the calculated lower and upper limits for the proportion.

## Product P and Profitability Analysis I

Suppose you are a manager in P Manufacturing that makes Product P only. The demands for Product P are 100 units per week at \$90 per unit. The overhead (fixed) cost is \$3,000 that includes \$1,500 of operators' salaries, \$1,000 equipment depreciation and \$500 of utilities.

There are two raw materials: Steel Widget and Metal Bracket for products P. The unit costs for raw materials are \$25.00 and \$20.00 for Steel Widget, and Metal Bracket, respectively.

You are going to decide how many Ps to make in order to break-even (the net profit is zero) for the company

Breakeven(Units)=FixedCost /(SellingPrice-VariableCost)=\$3000/(\$90-\$45)

 $Profit / Loss = \$90 \times DemandD - \$3,000 - \$45 \times DemandD$ 



You may want to Pause the Video to open Excel@ file LectureSIM.xls before continue



#### Set Excel@ Manual calculations of formulas and Press F9 to recalculate

Remember to Press F9 to recalculate

Your computer may work really slow if you do not set up Manual calculations of formulas when doing simulation.

Remember to set it back to automatic when finish simulations.





Using Excel@ to calculate Breakeven Point:

Set up Excel@ formulas to calculate Profit/Loss:

	А	В	С	D	E	F	G	Н	I.
9	Wk Demand D	100				- 			
10									
11			=\$B\$4	=\$B\$5	75	=\$B\$7	=C13*E13	=F13+D13*E13	=G13-H13
12	No.		Sell Price sp	Unit Cost v	Wk Demand D	Fixed Cost FC	Revenue	Total Cost	Profit/Loss
13	1								
40	Ne		Call Daise as	Unit Control	Wh Demond D	Fined Cost FC	Deve	Tatal Cast	Destitutes
12	NO.		Sell Price sp	Unit Cost V	WK Demand D	Fixed Cost FC	Revenue	Total Cost	Profit/Loss
13	1		90	45	75	3000	6750	6375	375.00
14	2		90	45	50	3000	4500	5250	(750.00)
15	3		90	<u>45</u>	<u>100</u>	3000	9000	7500	<u>1500.00</u>

#### Use of One and Two Variable Data Tables in Excel@ for Sensitivity Analysis

2/25/2009





## Calculate Mean and Standard Deviation of Profit and Percentage of Loss

	А	В	С	Н	I.	J K	L	М	N
1	Exercise 1: Sim	ple Simulat	tion Proce						
2			Breakeve			n	3	=COUNT(I	13:115)
3			Flip Two			Average Profit	375.00	=AVERAG	E(113:115)
4	Sell Price sp	Il Price sp 90 HH				Standard Deviation	1125	=STDEV(I1	3:115)
5	Unit Cost v	45	HT, T			Standard Error	649.52	=L4/SQRT	L2)
6			Π			t Critical Value	4.303	=TINV(0.0	5,L2-1)
7	Fixed Cost FC	3000				Margin of Error	2794.65	=L6*L5	
8						95% CI Lower Limit	(2419.65)	=L3-L7	
9	Wk Demand D	100				95% CI Upper Limit	3169.65	=L3+L7	
10									
11			=\$B\$	=F13+D13*E13	=G13-H13	No. of losses	1	=COUNTIF	(113:115,"<0")
12	No.		Sell Pric	Total Cost	Profit/Loss	Possibility of loss	0.3333	=L11/L2	
13	1		90	6375	375.00	Standard deviation of loss	0.2722	=SQRT(L12	2*(1-L12)/L2)
14	2		90	5250	(750.00)	z critical value	1.960	=NORMSI	VV(0.975)
15	3		90	7500	1500.00	Margin of Error of loss	0.5334	=L14*L13	
			-			95% CI Lower Limit of % loss	-0.2001	=L12-L15	
						95% CI Upper Limit of % loss	0.8668	=L12+L15	

	А	В	С	D	E			F	G	Н	- I	
1	Exercise 2: Use	of Rand	lom Number	Generation	in Simulati	ion						
2			Breakeven fo	r Product P								Lles Discrete
3			Flip Two Coir	Chance	From Pr	ob	٦	To Prob	Wk Demar	nd D		Use Discrete
4	Sell Price sp	90	HH	0.25	0			0.25	100			Probability in
5	Unit Cost v	45	HT, TH	0.50	0.25			0.75	75			simulation
6			Π	0.25	0.75			1.00	50			
7	Fixed Cost FC	3000					个					-
8												-
9	Wk Demand D	100										-
10												_
11												_
12	No.		Sell Price sp	Unit Cost v	Wk Dema	nd D	Fite	ed Cost FC	Revenue	Total Cost	Profit/Loss	_
13	1	0.6589	90	45	75			3000	6750	6375	375.00	Fveball
14	14 2 0.8656		90	45	50			3000	4500	5250	(750.00)	
15	3	0.1365	90	45	100			3000	9000	7500	1500.00	_
16					=VLOOKU	P(B18	,\$E\$	4:\$G\$6,3)				_
17	No.		Sell Price sp	Unit Cost v	Wk Dema	nd D	Fixe	ed Cost FC	Revenue	Total Cost	Profit/Loss	
18	4	0.6589	90	45	75			3000	6750	6375	375.00	= =VLOOKUP()
19	5	0.8656	90	45	50			3000	4500	5250	(750.00)	with given
20	6	0.1365	90	45	100			3000	9000	7500	1500.00	
		I RED		К	L	Ν	Л		N			random
<u>_ π</u>		I DLZ			No.1-3	No.	4-6					numbers
			n		3	3	3	=COUNT(	(118:120)			
			Average	Profit	375.00	375	.00	=AVERAG	GE(118:120)	Collo	at atatic	tics for the
			Standard	d Deviation	1125	11	25	=STDEV(I	18:120)	Colle	LE SEALIS	lics for the
			Standard	d Error	649.52	649	.52	=M4/SQF	RT(M2)	mear	n and sta	andard
		t Critical	Value	4.303	4.3	303	=TINV(0.	05,M2-1)	dovia	tion of	profit and	
		Margin o	Margin of Error 2		2794	4.65	=M6*M5					
			95% CI L	95% CI Lower Limit (2		(2419	9.65	) =M3-M7		the n	umber (	ot losses
10 - 11			95% CI U	pper Limit	3169.65 3169.6		9.65	=M3+M7				
/25/2	2009			Simulat	ion lecture	e note	es b	y Dr. Ping	vvang			8

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	Α	В	С	D	E	F	G	Н	I
1	Exercise 2: Use	e of Rando	om Number Ge	eneration in	Simulation				
2			Breakeven fo	or Product P					
3			Flip Two Coir	Chance 👕	From Prob	To Prob	Wk Deman	d D	
4	Sell Price sp	90	HH	0.25	0	0.25	100		
5	Unit Cost v	45	HT, TH	0.50	0.25	0.75	75		
6			Π	0.25	0.75	1.00	50		
7	Fixed Cost FC	3000				T			
8									
9	Wk Demand D	100							
10									
11									
12	No.		Sell Price sp	Unit Cost v	Wk Demand D	F xed Cost FC	Revenue	Total Cost	Profit/Loss
13	1	0.6589	90	45	75	3000	6750	6375	375.00
14	2	0.8656	90	45	50	3000	4500	5250	(750.00)
15	3	0.1365	90	45	100	3000	9000	7500	1500.00
16					=VLOOKUP(B18	, 3E\$4:\$G\$6,3)			
17	No.		Sell Price sp	Unit Cost v	Wk Demand D	ixed Cost FC	Revenue	Total Cost	Profit/Loss
18	4	0.6589	90	45	75	3000	6750	6375	375.00
19	5	0.8656	90	45	50	3000	4500	5250	(750.00)
20	6	0.1365	90	45	100	3000	9000	7500	1500.00
21					=VLOOKUP(B23	,\$E\$4:\$G\$6,3)			
22	No.	=RAND()	Sell Price sp	Unit Cost v	Wk Demand D	Fixed Cost FC	Revenue	Total Cost	Profit/Loss
23	7	0.9181	90	45	50	3000	4500	5250	(750.00)
24	8	0.1763	90	45	100	3000	9000	7500	1500.00
25	9	0.5888	90	45	75	3000	6750	6375	375.00

=VLOOKUP() with given random numbers

=VLOOKUP() with =RAND()

ATM ATM1 BE1 BE2 BE3 🧶

Use random number generator in simulation

J	К	L	М	N	0	
		No.1-3	No.4-6	No.7-9		
	n	3	3	3	=COUNT(123:125)	
	Average Profit	375.00	375.00	750.00	=AVERAGE(123:125)	
	Standard Deviation	1125	1125	649.5191		
	Standard Error	649.52	649.52	375.00		
	t Critical Value	4.303	4.303	4.303		
	Margin of Error	2794.65	2794.65	1613.49		
	95% CI Lower Limit	(2419.65)	(2419.65)	(863.49)		
	95% CI Upper Limit	3169.65	3169.65	2363.49		

	А	В	С	D	E		F		G		Н			1		
1	Exercise 2: Use	of Rando	om Number G	eneration in	Simu	lation									T	
2			Breakeven fo	or Product P								Цc	n ra	ndo	m	numbor
3			Flip Two Coir	Chance	Fro	om Prob	To Pro	b	Wk De	eman	d D	030		muc	711	number
4	Sell Price sp	90	нн	0.25		0	0.25		10	0		ger	nera	ator	in	simulation
5	Unit Cost v	45	HT, TH	0.50		0.25	0.75		75	5						
6			Π	0.25		0.75	1.00		50	D						
7	Fixed Cost FC	3000				T										
8							v		1	D	4	N		0	1	D
9	Wk Demand D	100					r.		L		VI	IN				۲
10								N	0.1-3	NO.	.4-6	No.	/-9	No.10	)-12	
11						n			3		3	3		3		=COUNT(128:130)
12	No.		Sell Price sp	Unit Cost v	Wk	Aver ige	Profit	37	5.00	375	.00	375.	00	750.0	)	=AVERAGE(128:130)
13	1	0.6589	90	45		Stan dard	Deviation	1	125	11	.25	112	25	649.5	191	
14	2	0.8656	90	45		Star dard	Frror	64	9.52	649	9.52	649	52	37		
15	3	0.1365	90	45		t Critical I	Value	4	202	4.2	002	4.2	02	1 20		
16					=VL(			4	.505	4.3	505	4.5	05	4.50	P	
17	No.		Sell Price sp	Unit Cost v	Wkl	Margin of	f Error	27	94.65	279	4.65	2794	.65	1613.	.95	
18	4	0.6589	90	45		95 % CI Lo	wer Limit	(24)	19.65)	(241	9.65)	(2419	9.65)	(863.	<del>1</del> 9)	
19	5	0.8656	90	45		95 % CI Up	oper Limit	316	i9.65	3169	9.65	3169	.65	2363	49	
20	6	0.1365	90	45	-	100	0000		500	50	73	00	1.00	00.00	+	
21					=VLC	OKUP(B2	3,\$E\$4:\$G\$6	6,3)							_	
22	No.	=RAND()	Sell Price sp	Unit Cost v	WkD	emand D	Fixed Cos	t FC	Reve	nue	Total	Cost	Prof	it/Los	5 _	
23	7	0.5963	90	45		75	3000		675	50	63	75	37	5.00		-VLOOKOP()
24	8	0.7780	90	45		50	3000		450	00	52	50	(75	50.00)	– v	with =RAND()
25	9	0.1635	90	45		100	3000		900	00	75	00	150	00.00	_	
26					=VLC	OKUP(RA	ND(),ŞEŞ4:	ŞGŞê	5,3)				_		-	
27	No.		Sell Price sp	Unit Cost v	Wk D	emand D	Fixed Cos	t FC	Reve	nue	Total	Cost	Prof	it/Los	5	
28	10		90	45		100	3000		900	00	75	00	150	0.00	+	
29	11		90	45		75	3000		675	50	63	75	37	5.00	+	
30	12		90	45		50	3000		450	00	52	50	(75	0.00)	1	
7		BE1 BE2	BE3 P								52		(75		-	

## =VLOOKUP(RAND())

2/25/2009

Simulation lecture notes by Dr. Ping Wang

											4
		А	В	С	D	E	F	G	н	- I	
	1	Exercise 3		Breakeven fo	r Product P						14 !
	2			Flip Two Coins	Chance	From Prob	To Prob	Wk Demar	nd D		It is very
	3	Sell Price sp	90	HH	0.25	0	0.25	100			
	4	Unit Cost v	45	HT, TH	0.50	0.25	0.75	75			usetul to
	5			Π	0.25	0.75	1.00	50			I
	6	Fixed Cost F	3000			- 7					nave a rew
	7						<b>T</b>				
	8	Demand D	100								rows
	9										· · · <b>:</b> • • • • • • • • • • • • • • • • • • •
	10										without
	11	No.		Sell Price sp	Unit Cost v	Wk Demand D	Fixed Cost FC	Revenue	Total Cost	Profit/Loss	randam
	12		0.658912	90	45	75	3000	6750	6375	375.00	ranuom
	13		0.86555	90	45	50	3000	4500 🔎	5250	(750.00)	numbers to
	14		0.136484	90	45	100	3000	9000	7500	1500.00	numbers to
	15					=VLOOKUP(RA	NE (),\$E\$3:\$G\$5	,3)			vorify
	16	1		90	45	50	3000	4500	5250	(750.00)	verny
	17	2		90	45	50	3000	4500	5250	(750.00)	corroctaocc
	18	3		90	45	50	3000	4500	5250	(750.00)	correctness
	19	4		90	45	75	3000	6750	6375	375.00	of formulac
	20	5		90	45	75	3000	6750	6375	375.00	oriormulas
h		^	P	C	D	E	E	G			Г
1	113	98	0	90	45	75	3000	6750	6375	375.00	
1	114	99		90	45	75	3000	6750	6375	375.00	
1	115	100		90	45	75	3000	6750	6375	375.00	
1	116	101		90	45	50	3000	4500	5250	(750.00)	
1	117	102		90	45	50	3000	4500	5250	(750.00)	
		-	_		_						F
		A	В	C	D	E	F	G	H	(750.00)	
-	512	496		90	45	100	3000	4500	5250	(750.00)	
-	512	497		90	45	100	3000	9000	7500	1500.00	
-	514	499		90	45	75	3000	6750	6375	375.00	
5	515	500		90	45	75	3000	6750	6375	375.00	
5	516					=VLOOKUP(RA	ND(),\$E\$3:\$G\$5	,3)			
	-										

# Double verify the correctness of equations in the first and last rows before production runs of the simulation

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	А	В	С	D		E		F	G		Н	I	J	К	L
1	Exercise 3		Breakev	E										n	=COUNT(I12:I14)
2			p Two Co	i Chance		From	Prob	To Prob	Wk Deman	c				Average Profit	=AVERAGE(I12:I14)
3	Sell Price s	90	HH	0.25	0			=D3	100					Standard Deviation	=STDEV(112:114)
4	Unit Cost v	=25+20	HT, TH	0.5	=F3			=F3+D4	75					Standard Error	=L3/SQRT(L1)
5			Π	0.25	=F4			=F4+D5	50					t Critical Value	=TINV(0.05,L1-1)
6	Fixed Cost I	3000												Margin of Error	=L5*L4
7														95% CI Lower Limit	=L2-L6
8	Demand D	100												95% CI Upper Limit	=L2+L6
9															
10														No. of losses	
11	No.		ell Price s	Unit Cost	Wk D	emand D		xed Cost	Revenue	То	tal Cost	Profit/Loss		Possibility of loss	
12		0.658911	=\$B\$3	=\$B\$4	75			=\$B\$6	=C12*E12	=F12+	D12*E12	=G12-H12		Standard deviation of loss	
13		0.865550	=\$B\$3	=\$B\$4	50			=\$B\$6	=C13*E13	=F13+	D13*E13	=G13-H13		z critical value	
14		0.136484	=\$B\$3	=\$B\$4	100			=\$B\$6	=C14*E14	=F14+	D14*E14	=G14-H14		Margin of Error of loss	
15					=VLO	OKUP(RAND	(),\$E\$3:\$G\$5,3)							95% CI Lower Limit of % loss	
16	1		=\$B\$3	=\$B\$4	=VLO	OKUP(RAND	(),\$E\$3:\$G\$5,3)	=\$B\$6	=C16*E16	=F16+	D16*E16	=G16-H16		95% CI Upper Limit of % loss	
17	2		=\$B\$3	=\$B\$4	=VLO	OKUP(RAND	(),\$E\$3:\$G\$5,3)	=\$B\$6	=C17*E17	=F17+	D17*E17	=G17-H17			

Use Formulas/Show formulas or CTRL+` to show formulas in Excel@ worksheet Additional adjustment to column width may be needed and use Print Preview/Page setup/Fit into 1 or 2 pages to produce professional printouts.



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1	Instruction	s:										Examples:			
0 Q	1 Put all N	formulas	vou want	to simula	te next to	each other or	eceded by	v the nu	mber of	trials you wan	nt to run	a) Select ran	ne I11·K13· press	Ctrl+W	
10	i. i ucui ii	Ionnaiao	you want	to simala	to next to	cuen other, pr	cecucu b	y the ha	moer or	thats you wan	it to run.	a) ociect fait	gerrinitio, press	ourivi.	
11	2. Select th	e N+1 ce	lls and th	e 7x(N+1)	cells bene	ath (indicated	by frame	).					100	0.5765	0.1551
12					K										
13	3. Run mac	ro "simul	ate" or pr	ess Ctrl+V	V to run sir	mulation. Res	ult:		_						
14			•			17001.00									
15		100	0		0.8558	1/284.63	338	0.44	84			b) Calastan		Chilly M/ (a many supplie	a a la constituit de la constante
10		Sta	an and arro	hr.	0.0030	2190.00	36	-0.01	09			b) Select ran	ige 110.JZ I, press i	CIN+VV (a new workd	ook will be create
18		Med	dian		0 4878	186 13	393	-0.01	74				1000	-0 946874983	
19		Sta	ndard dev	iatic	0.2986	4290.00	502	0.97	61				0.000		
20		Var	iance		0.0891	18404616.81	190	0.95	29						
21		Ske	wness		0.0039	2.48	379	0.04	73						
22		Kur	tosis		1.7135	8.75	563	2.95	63						
23				/		/									
24	Note:			K											1
26	- If the num	ber of tria	ls is neoa	ative, simu	lation is ru	n in high-spee	d mode w	ith mini	mized w	indows.					
27	7 - If the cell with the number of trials has bold font type, histograms are created at end of simulation run.														
28	- If you sele	ect less th	an 7 rows	s of cells b	eneath for	mulas, you ge	t less out	put.							
2/2	5/2009					Sim	ulatio	n lecti	ure no	otes by Dr	How	to use I	MonteCa	rlito	14

## Use MonteCarlito in simulation

	- I	J		Κ		L	М	N	0	Р		QR		S	
1			n			3	10	100	500	40	0	400			
2			Average	Pro	ofit	375.00	150.00	262.50	395.25	428.	44	375.70	=L21		
3			Standard	De	eviation	1125	887.4119675	775.15	816.48	824	. <mark>08</mark>				
4			Standard	Eri	ror	649.52	280.62	77.51	36.51	41.	20	36.19	=L24		
5			t Critical	Val	lue	4.303	2.262	1.98	1 96	1.9	7	1.97	=TINV(0	).05,R1-1)	
6			Margin o	f Er	ror	2794.65	634.82	153.81	/1.74	81.	00	71.14	*R5*R4		
7			95% CI Lo	we	er Limit	(2419.65)	(484.82)	108.69	323.51	347.	43	304.56	=R2-R6		
8			95% CI U	ppe	er Limit	3169.65	784.82	416.31	466.99	509.	44	446.85	=R?+R6		
9															
10			No. of lo	sse	s						-	100.00	±M2.		
11	Profit/Loss		Possibili	ty c	of loss							0.2500	= R10/ R1		
12	375.00		Standard	de	viation	of loss						0.0217	=SQRT F	R11*(1-R11	)/R1)
13	(750.00)		z critical	val	ue							1.960	=NORM	5INV(0.975	5)
14	1500.00		Margin o	f Er	rror of lo	SS						0.0424	=R13*R1	L	
15			95% CI Lo	owe	er Limit o	of % loss						0.207566	=R1R1	.4	
16	375.00		95% CI U	ppe	er Limit o	of % loss						0.2924	=R11+R1	14	
17	375.00										_				
18	375.00		MonteCa	rlit	to	=P2	=COUNTIF(I1	16:1515,"	<0")	18		MonteCarli	to	=12	=COUNTIF(I11
19	1500.00					AvgPr fit	No. of Loss	Z		19				AvgPi ofit	No. of Loss
20	375.00	1	-	16		428.44	98			20	1	-16		428.44	98
21	(750.00)	2			Monte	arlito	=P2	COUNTI	F(1116	21	2	Mean	$\star$	375.70	100.00
22	(750.00)	3					AveProfit	No. of L	055	22	3	Standard er	ror	9.05	1.81
23	1500.00	4		1		-16	428.44	98	_	23	4	Median		369.38	101.00
24	(750.00)	5		2		10	120.11	50	- I	24	5	Standard de	viation	36.19	7.25
25	(750.00)	6		2					- I-	25	6	Variance		1309.63	52.50
26	(750.00)	7		2					- I-			ſ			i i i i i i i i i i i i i i i i i i i
27	(750.00)	8		4											
H -	I 🕨 🖬 📈 Po	rtC	om1 🖉 B	5					A	TM1	BE	E1 / BE2 B	E3 BE4	2	
				6						Dra	~~	ОТО	. \\/ +.		to Corlita
				7						-16	22		+ • • • • •		levanilo

																r
	Α	В	С		D		E	F			G		H	1	1	
1	Exercise 3		Breakeven for	r Pi	roduct P		-									
2			Flip Two Coins		Chance	Fror	n Prob	To Pro	b	Wk	Dem	and D	_			
3	Sell Price sp	90	HH		0.25		0	0.25			100		_			
4	Unit Cost v	45	нт, тн		0.50 0.		0.25	0.75			75		_			
5			Π		0.25	0	).75	1.00			50					
6	Fixed Cost F	3000		_									_			
/	D	400		J	K		L	М	N		0	Р	0	R		S
8	Demand D	100					2	10	100	<b>`</b>	500	400	T	400		
9					n		3	10	100	)	200	400	_	400		
10	No.		Sell Price sp		Average Pr	rofit	375.00	375.00	510.0	0 43	33.50	414.38		379.47	=L21	
12		0.658912	90		Standard D	eviation	1125	530.3300859	771.	51 7	97.32	803.45				
13		0.86555	90		Standard F	rror	649 52	167 71	77 1	5 2	15 66	/0 17		44 19	-1.24	
14		0.136484	90	-	Stanuaru L		045.52	107.71	//.1	.5 5	5.00	40.17	+	44.17	-L24	
15					t Critical V	alue	4.303	2.262	1.9	8   3	1.96	1.97		1.97	=TINV(0.0	5,R1-1)
10	2		90		Margin of I	Error	2794.65	379.38	153.0	08 7	70.06	78.98		86.88	=R5*R4	
18	3		90		95% CLLow	or Limit	(2419.65)	(4.38)	356.9	12 36	53 //	335 //0		292 59	-R2-R6	
19	4		90		5570 CT LOW	/er cinin	(2415.05)	(4.50)	550.5	12 30	JJ.44	333.40	+	232.33	-112-110	
20	5		90		95% CI Upp	oer Limit	3169.65	754.38	663.0	08 50	03.56	493.35		466.35	=R2+R6	
	А	В	С		No. of loss	05								05		(1116-1515 "20")
113	98		90		100.011055	65							+	55	-0000	(1110.1515, <0.)
114	99		90		Possibility	of loss								0.2375	=R10/R1	
115	100		90		Standard d	eviation	of loss							0.0213	=SORT(R1)	1*(1-R11)/R1)
117	101		90		z critical va	ماليم								1 960		NV(0.975)
				-	2 citical ve	nue							+	1.500	-NORMON	10,010
	Α	В	С		Margin of I	Error of lo	SS							0.0417	=R13*R12	
511	496		90		95% CI Low	/er Limit d	of % loss							0.19579	7 =R11-R14	
512	497		90		05% (111)	orlimite	of % loss						+	0 2702	-011+014	
513	498		90	_	33% CI Upp	er Limit (	01 % 1055						_	0.2792	=K11+K14	
514	499		90		45		75	3000		6	5750	6	53	75	375.00	
515	500		90		45 7		75	3000		6	5750	6	53	75	375.00	
516					=VLOC		OKUP(RA	ND(),\$E\$3:\$	\$G\$5,	,3)						

#### Final result of the simulation with MonteCarlito

	J	К	L	М	N	0	Р	QR	S	
1		n	3	10	100	500	400	400		$X \perp \zeta, S_{\pm}$
2		Average Profit	375.00	375.00	476.25	375.00	349.69	379.47	=L21	J X
3		Standard Deviation	1125	918.5586535	784.90	815.18	821.58			We are 95% sure
4		Standard Error	649.52	290.47	78.49	36.46	41.05	44.19	=L24	that the unknown
5		t Critical Value	4.303	2.262	1.98	1.96	1,57	1.97	=TINV(0.05,R1-1)	that the unknown
6		Margin of Error	2794.65	657.10	155.74	71.63	<b>50.7</b> 6	86.88	=R5*R4	true average profit is
7		95% CI Lower Limit	(2419.65)	(282.10)	320.51	303.37	265.93	292.59	=R2-R6	hetween 292 59 and
8		95% CI Upper Limit	3169.65	1032.10	631.99	446.63	.30.45	466.35	=R2+R6	
9										466.35.
10		No. of losses						99.41	=M21	
11		Possibility of loss						0.2485	=R10/R1	
12		Standard deviation	of loss					0.0216	=SQRT(R11*(1-R1	1)/R1)
13		z critical value						1.960	=NORMSINV(0.97	5)
14		Margin of Error of lo	SS					0.0424	=R13*R12	
15		95% CI Lower Limit of	of % loss					0.206174	=R11-R14	
16		95% CI Upper Limit o	of % loss					0.2909	=R11+R14	
17										
18		MonteCarlito	=P2	=COUNTIF(I1	16:1515,"	<0")				
19			Avg	loss			-	$\overline{n} +$	$7\sqrt{n}$	$1 - \overline{n} / n$
20	1	-100	349.69	111					$L \setminus D$	1 - D / N
21	2	Mean	379.47	99.41				-		$\mathbf{I}$
22	3	Standard error	4.42	0.94			14/	OF		
23	4	Median	377.81	100.00			VV	e are 95	5% sure that	the unknown
24	5	Standard deviation	44.19	9.36			trı	le possi	bility of loss	s is between
25	6	Variance	1952.87	87.56			20	670/ ~	, , ,	
26	7						20	.02% di	iu 29.09%.	

## How to interpret simulation results?



	_		-		-							
	J	К	L	М	N	0	Р	Q	R )	R	S	
1	-	n	3	10	100	500	400		400	400		$X \perp \zeta, S \equiv$
2		Average Profit	375.00	375.00	476.25	375.00	349.69		379.47	373.62	K	S X
3		Standard Deviation	1125	918.5586535	784.90	815.18	821.58	Ι				We are 95% sure
4		Standard Error	649.52	290.47	78.49	36.46	41.08		44.19	45.74		that the unknown
5		t Critical Value	4.303	2.262	1.98	1.96	1/57		1.97	1.97	5,R1-1)	
6		Margin of Error	2794.65	657.10	155.74	71.63	<b>50.7</b> ó		86.88	89.93		true average profit is
7		95% CI Lower Limit	(2419.65)	(282.10)	320.51	303.37	265.93		292.59	283.69		hetween 283 69 and
8		95% CI Upper Limit	3169.65	1032.10	631.99	446.63	.30.45		466.35	463.55		
9												463.55.
10		No. of losses							99.41	140.45		
11		Possibility of loss						Ζ	0.2485	0.3511	K	
12		Standard deviation	of loss						0.0216	0.0239	.*(1-R1	1)/R1)
13		z critical value							1.960	1.960	IV(0.97	5)
14		Margin of Error of lo	SS						0.0424	0.0468		
15		95% CI Lower Limit of	of % loss						0.206174	0.304348		
16		95% CI Upper Limit o	of % loss						0.2909	0.3979	[	
17										F		
18		MonteCarlito	=P2	=COUNTIF(I1	16:1515,"	<0")						
19			Avg	loss				r		71	$\overline{n}$	$- \overline{n} / n$
20	1	-100	349.69	111				V	/ /	ζ. V	$\mathcal{V}$	1 - D / N
21	2	Mean	379.47	99.41				4		V		
22	3	Standard error	4.42	0.94			1.4/			0/ 01/10	that	the uplus our
23	4	Median	377.81	100.00			VV	e	are 95	% sure	e that	the unknown
24	5	Standard deviation	44.19	9.36			trı	ue	possi	bility o	of loss	s is between
25	6	Variance	1952.87	87.56			20		120/ an	, 7 0 C h	00/	
26	7	1					30	J.4	12 /0 dl	iu 39.7	970.	

## Less profit and more loss due to more variations

				=AVERA	GE(C116	:C515)								
	MonteCarlito	=P2	=COUNTIF(I1:	16:I515,"	<0")									
		AvgProfit	loss	AvgSPrc	AvgUCt									
1	-100	391.82	140	90.08	44.99	=AVERA	GE(D116:D5	15)						
2	Mean	373.62	140.45											
3	Standard error	4.57	1.02											
4	Median	374.01	139.00											
5	Standard deviation	45.74	10.20											
6	Variance	2092.34	104.13											
7														
1	i	Press C	Press CTRL+W to get Result											

#### Use MonteCarlito to collect statistics for multiple performance measures



IF D<=Q, THEN SOLD = D, INV LEVEL=Q-D, INV COST=Ci (Q-D) ELSE SOLD = Q, LOST SALES=D-Q, LOSS COST = CI (D-Q)

PROFIT/LOSS = PRICE \* SOLD - INV COST – LOSS COST

In Excel@, use either SOLD=IF(D<=Q,D,Q) or SOLD=MIN(D,Q) For any leftover, use either LEFTOVER=IF(D<=Q,Q-D,0) or LEFTOVER=MAX(Q-D,0) For any lostsale, use either LOSTSALE=IF(D<=Q,0,D-Q) or LOSTSALE=MAX(D-Q,0)

Calculate INVCOST=IF(D<=Q,HoldCost\*(Q-D),0) or INVCOST=MAX(HoldCost\*(Q-D),0) And SHORTCOST=IF(D<=Q,0,ShortUC\*(D-Q)) or SHORTCOST=MAX(ShortUC\*(D-Q),0)

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## Use =IF(), =MIN(), and =MAX() in Inventory simulation

	Α	В	С	D	E	F	G	Н	- I	
1	Given	Inventory level Q	100		Demand Mean	100				
2		Unit Inventory holding cost	15		Demand Std	20				
3		Unit Shortage cost	30							
4		Sales price	125							
5		Unit cost	75							
6		Gross Profit /unit	50							
7										
8		1. If D <= Q, then D units are	sold, Q - D uni	its leftover						
9		<ol><li>If D &gt; Q, then Q units are s</li></ol>	old, D - Q unit	s are shotages						
10		Excel formulas to compute l	Units sold, Uni	ts leftover and U	Inits shortages					
11										
12		Demand (D)	Normal (100,	20)	=ROUND(NORN	IINV(RAND(),10	0,20),0)			
13		Units sold	If (D <= Q, D, 0	ב)	=IF(B26<=\$C\$1,	B26,\$C\$1)	=MIN(B26,\$C\$1	)		
14		Units leftover	If (D <q, -="" d<="" q="" td=""><td>, 0)</td><td>=IF(B26&lt;\$C\$1,\$</td><td>C\$1-B26,0)</td><td>=MAX(\$C\$1-B20</td><td>5,0)</td><td></td><td></td></q,>	, 0)	=IF(B26<\$C\$1,\$	C\$1-B26,0)	=MAX(\$C\$1-B20	5,0)		
15		Units shortage	If (D > Q, D - 0	2, 0)	=IF(B26>\$C\$1,B	26-\$C\$1,0)	=MAX(B26-\$C\$	1,0)		
16										
17		Net Profit = Gross Profit * Ur	nits Sold - Inve	entory holding co	ost * Units leftov	er - Shortage co	st * Units shorta	iges		
18			=\$C\$6*C26-\$0	\$2*D26-\$C\$3*F	26					
19		Inventory Cost	Unit Inventor	y holding cost *	Units leftover	=\$C\$2*D26				
20		Shortage Cost	Unit shortage	cost * Units sho	rtage	=F26*\$C\$3				
21			=IF(B24<=\$C\$	1,B24,\$C\$1)	=\$C\$2*D24		=F24*\$C\$3			
22		=ROUND(NORMINV(RAND()	,\$F\$1,\$F\$2),0)	=IF(B24<\$C\$1,\$	C\$1-B24,0)	=IF(B24>\$C\$1,B	24-\$C\$1,0)	=\$C\$6*C24	E24-G24	4
23	No.	Demand (D)	Units Sold	Units Leftover	Inventory Cost	Units Shortage	Shortage Cost	Net Profit		
24	1	108	100	0	0	8	240	4760		
25	2	73	73	27	405	0	0	4055		_
26	3	95	95	5	75	0	0	4825		_
27	4	119	100	0	0	19	570	4430		_
28				=MAX(\$C\$1-B30	),0)		=F30*\$C\$3			4
29			=MIN(B30,\$C	\$1)	=\$C\$2*D30	=MAX(B30-\$C\$1	X(B30-\$C\$1,0) =\$C\$6*C		E30-G3	D
30	5	115	100	0	0	15	450	4550		
31	6	88	88	12	180	0	0	4580		4
32	7	116 Pagedale12_2PortCom	100	0 PorCom2 / Port/	0 Com1 Rutler	16 TutorButler	480	4520		
Ragsdale12_2 / Portcom / Portcom2 / Portcom3 / Portcom1 / Butler / Butler / Butler / Butler / ATMBlank / ATM										

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Example of Simulation	Process for	Inventory	Levels

	А	В	С	D	E	F	G	Н		J	К	L	М	Ν	0
1	Butler invento	iry		Selling Price		\$125									
2				Unit Cost		\$75									
3	Gross Profit pe	er Unit	\$50												
4	Holding Cost p	er Unit	\$15		Summary Statist	tics			<b>Relationships</b> am	ong Q, Average	Net Profit (\$) and	d Service Le	evel (%)		
5	Shortage Cost	per Unit	\$30		Mean Profit	\$4,508	=AVERAGE(G11	7:G316)	Replenishment	Average	Service	4,600 -			
6					Std Deviation	1286	=STDEV(G117:G	316)	Level Q	Net Profit (\$)	Level (%)	4,550 -		_	
7	Replenishmer	t Level Q	140		Min Profit	\$539	=MIN(G117:G31	6)	100	4,249	92.02%	4,500 -			
8					Max Profit	\$6,992	=MAX(G117:G31	.6)	105	4,366	94.20%	4,450 -			
9	Demand (Norr	nal Distribu	tion)		Service Level	99.92%	=C15/B15		110	4,456	96.38%	4,400 -	_//		
10	Mean	100			Std Error	\$91	=F6/SQRT(COUN	NT(G117:G3	3 115	4,523	97.27%	4,350 -			
11	Std Deviation	20	=SUM(C1	17:C316)					<u>120</u>	<u>4,545</u>	<u>98.55%</u>	4,300 -			t Profit (\$)
12		=SUM(B17:	B316)		=IF(B17<=\$C\$7,\$	C\$4*(\$C\$7-B17),	0)		125	4,534	99.02%	4,250	(		el (%)
13			=IF(B17<	=\$C\$7,B17,\$C\$	\$7)				130	4,475	99.40%	4,200 -		1	
14	Simulation	=NORMINV	(RAND(),	\$B\$10,\$B\$11)		=IF(B17>\$C\$7,\$0	C\$5*(B17-\$C\$7),0	)	135	4,419	99.68%	10	0 11	0 120	130
15	Total	30365	30342	=\$C\$3*C17			=D17-E17-F17		140	4,403	99.76%		R	eplenishmer	t Level Q
16	Month	Demand	sales	Gross Profit	Holding Cost	Shortage Cost	Net Profit								
17	1	95	95	\$4,760	672	0	\$4,088								
18	2	114	114	\$5,714	386	0	\$5,328		MonteCarlito	=F5	=F9				
19	3	62	62	\$3,098	1171	0	\$1,927			AvgProfit	AvgSvrLevel				
20	4	79	79	\$3,944	917	0	\$3,027	1	-10	4508.34	0.9992				
21	5	79	79	\$3,974	908	0	\$3,066	2	Mean	4403.06	99.76%				
22	6	121	121	\$6,057	283	0	\$5,774	3	Standard error	38.25	0.00				
23	7	87	87	\$4,356	793	0	\$3,562	4	Median	4397.97	1.00				
24	8	97	97	\$4,844	647	0	\$4,197	5	Standard deviation	120.96	0.00				
25	9	85	85	\$4,247	826	0	\$3,421	6	Variance	14630.83	0.00				
26	10	110	110	\$5,523	443	0	\$5,079	7							
27	11	125	125	\$6,247	226	0	\$6,021								
н	🕩 H 🖌 PortC	om1 / Butle	er 🖉 Tuto	rButler Butle	er1 ATMBlank	ATM ATM1	BE1 / BE2 / BE3	/ BE4 / 🤻							



2/25/2009 to Estimate Profit/Loss Simulation lecture notes by Dr. Ping Wang

## Case 5: Queue or Waiting Line



	А	В	С	D	E	F	G	Н	- I	J	К
1	Wachovia Bank	Dne ATM Sim	ulation Model					RN			

16	Initial Time	0																					
17	Simulation		=C21+B22																				
18		=\$B\$4+RAND()*(\$B\$5-\$B\$4) =D2				=NORMINV(H	13,\$F\$4,\$F\$5)																
19		Interarrival	Arrival	Service	Waiting	Service	Completion	Time															
20	Customer	Time	Time	Start Time	Time	Time	Time	in System	<b>RN For IATM</b>	RN For ST	z(RN SvrT)												
21	1	2	2	2	0	5	7	5															
22	2	1	3	7	4	3	10	7															
23	3	8	11	11	0	4	15.000	4															
24	4	3.926	14.926	15	0.0744	1.728	16.728	1.802	0.9814	0.2932	-0.5441												
25	5	2.189	17.115	17.115	0	1.294	18.409	1.294	0.5473	0.079	-1.4118												
26	6	1.224	18.339	18.409	0.070	2.359	20.768	2.429	0.306	0.7634	0.7173												
27	7	0.286	18.624	20.768	2.143	1.461	22.228	3.604	0.0714	0.1404	-1.0785												
H.	PortCor	n / PortCom2	/ PorCom3	PortCom1	Butler / Tuto	orButler / Butle	er1 🖉 ATMBlan	ATM AT	ГМ1 / BI 🛛 🔚		◆ ▶ PortCom / PortCom2 / PorCom3 / PortCom1 / Butler / TutorButler / Butler1 / ATMBlank ATM / ATM1 / B												

#### Sample Set up for Queuing or Waiting Line Simulation

	А	В	С	D	E	F	G	Н	I	J	K
1	Wachovia Bank	One ATM Sim	ulation Model	l				RN			
2								0.9814			
3	Interarrival Time	es (Uniform Di	istribution)		Service Times	s (Normal Dist	tribution)	0.2932			
4	Smallest Value	0			Mean	2		0.5473			
5	Largest Value	4			Std Deviation	0.5		0.079			
6								0.306			
7	RN	Interarrival T	ime					0.7634			
8	0.3693	1.4772	=\$B\$4+RAND	)*(\$B\$5-\$B\$4)	)			0.0714			
9								0.1404			
10											
11											
12	RN	Service Time									
13	0.7955	2.4128	=NORMINV(A	13,\$F\$4,\$F\$5)							
14											
15											
16	Initial Time	0									
17	Simulation		=C21+B22								
18		=\$B\$4+RAND	()*(\$B\$5-\$B\$4)	)	=D21-C21	=NORMINV(H	13,\$F\$4,\$F\$5)				
19		Interarrival	Arrival	Service	Waiting	Service	Completion	Time			
20	Customer	Time	Time	Start Time	Time	Time	Time	in System	RN For IATM	RN For ST	z(RN SvrT)
21	1	2	2	2	0	5	7	5			
22	2	1	3	7	4	3	10	7			
23	3	8	11	11	0	4	15.000	4			
24	4	3.926	14.926	15	0.0744	1.728	16.728	1.802	0.9814	0.2932	-0.5441
25	5	2.189	17.115	17.115	0	1.294	18.409	1.294	0.5473	0.079	-1.4118
26	6	1.224	18.339	18.409	0.070	2.359	20.768	2.429	0.306	0.7634	0.7173
27	7	0.286	18.624	20.768	2.143	1.461	22.228	3.604	0.0714	0.1404	-1.0785
н	PortCor	n 🖉 PortCom2	/ PorCom3 /	PortCom1 🖌	Butler 📈 Tuto	rButler 📈 Butl	er1 📈 ATMBlan	K ATM AT	FM1 🖌 🛛 🖣 📃		
Dat	a du										

#### Use a few easy examples to verify the logics before using random numbers

## The Process of Queuing or Waiting Line Simulation

	А	В	С	D	E	F	G	Н	I	J	K	L	М	Ν	0	Р
1	Wachovia Bank	One ATM Si	imulatio	n Model												
2					Summary Statis	stics										L
3	Interarrival Tin	nes (Uniform	n Distrib	ution)	Number Waitin	g	313	=COUNTIF(	E116:E615,">0")							
4	Smallest Value	0			Probability of V	Vaiting	62.60%	=G3/COUN	T(E116:E615)							
5	Largest Value	5			Average Waitin	ig Time	1.48	=AVERAGE	(E116:E615)							
6					Max Waiting Ti	me	8.59	=MAX(E116	i:E615)							
7	Service Times	Normal Dist	ribution	1)	Utilization of A	TM	80.93%	=SUM(F116	:F615)/(G615-G115)							
8	Mean	2			Number Waitin	ig >1 min	228	=COUNTIF(	E116:E615,">1")							
9	Std Deviation	0.5			Probability of V	Vaiting >1 min	0.4560	=G8/COUN	T(E116:E615)							
10				=IF(C17>G	16,C17,G16)											
11			=C16+B	17						M	onteCarlito					
12	Simulation	=\$B\$4+RAN	D()*(\$B\$	\$5-\$B\$4)		=NORMINV(RA	AND(),\$B\$8,\$I	B\$9)				AvgN Wait	AvgWTim	AvgMaxW	AvgUtil	AvgN Wait>1
13			=B16	=C16	=D16-C16		=D16+F16	=G16-C16		1	-10	313.00	1.48	8.59	80.93%	228
14		Interarrival	Arrival	Service	Waiting	Service	Completion	Time		2 M	ean	313.70	1.582009	10.466	0.799278	234.8
15	Customer	Time	Time	Start Time	Time	Time	Time	in System		3 Sta	andard error	5.24	0.093195	0.848036	0.005677	6.587564041
16	1	3.32	3.32	3.32	0.00	1.60	4.92	1.60		4 Me	edian	312.00	1.461297	9.286344	0.80084	228
17	2	0.65	3.96	4.92	0.95	2.94	7.86	3.90		5 Sta	andard deviati	16.56	0.29471	2.681727	0.017954	20.8317066
18	3	2.44	6.40	7.86	1.46	2.27	10.13	3.72		6 Va	riance	274.21	0.086854	7.191658	0.000322	433.96
19	4	4.19	10.59	10.59	0.00	2.59	13.19	2.59		7						
20	5	3.62	14.21	14.21	0.00	2.06	16.27	2.06								
21	6	2.47	16.69	16.69	0.00	1.16	17.84	1.16								
22	7	0.59	17.28	17.84	0.56	1.56	19.41	2.13								
23	8	3.47	20.75	20.75	0.00	0.88	21.63	0.88								
24	9	4.23	24.98	24.98	0.00	1.94	26.92	1.94								
25	10	1.69	26.67	26.92	0.25	2.58	29.50	2.83								
26	11	0.53	27.19	29.50	2.31	1.84	31.33	4.14								
27	12	0.52	27.71	31.33	3.62	2.68	34.02	6.30								
H.	🕩 M 🖌 PortCi	om1 / Butler	r 🖌 Tuto	orButler 🖌 E	Butler1 🖌 ATMBla	nk 🖉 ATM 🔪 AT	M1 / BE1 / B	E2 / BE3 /	BE4 🖉 🚺	•						
Rea	dv													田田1	00%	

## Simulation Overview:



The objectives of simulation:

To estimate the unknown population mean  $\mu_0$  (the average profit) and To estimate the unknown population proportion (of loss)

$$\overline{x} \pm z \, s_{\overline{x}} \qquad \overline{p} \pm z \, \sqrt{p} (1 - \overline{p})/n$$

Simulation as a tool in business decision making is very powerful, flexible and easy to use. Enjoy Simulating.