## Quiz Regression

A mail-order catalog business that sells personal computer supplies, software, and hardware maintain a centralized warehouse for the distribution of products ordered. Management is currently examining the process of distribution from the warehouse and is interested in studying the factors that affect warehouse distribution costs. Currently, a small handling fee is added to the order, regardless of the amount of the order. Data have been collected over the past 24 months indicating the warehouse distribution costs and the number of orders received. The results and the scatter plot for the Cost and Orders. Assume the Cost is the dependent variable (Y) and Orders is the independent variable (X). The Costs are in $\$ 1000$.

The Summary Output Table above is resulted from regression analysis with Orders as independent variable ( X ) and Costs as dependent variable ( Y ) to fit a linear trend model to the data set. Use the Table to answer the following questions:

1. Which one(s) of the following is not correct regarding $b_{l}$ ?
a. The $95 \%$ confidence interval is from 0.0131 to 0.0192
b. The costs will increase $\$ 16.10$ for each additional order received.
c. The slope of the regression line and is given by $=\operatorname{SLOPE}(\mathrm{D} 4: \mathrm{D} 27, \mathrm{C} 4: \mathrm{C} 27)$ in Excel@
d. Because the p-value is 0.0000 and is less than 0.05 , thus a non zero $b_{1}\left(\right.$ or $\left.b_{1} \neq 0\right)$ is confirmed.
2. Which one(s) of the following is not correct regarding $b_{0}$ ?
a. The Y intercept of the regression line and is given by $=\operatorname{INTERCEPT}(\mathrm{D} 4: \mathrm{D} 27, \mathrm{C} 4: \mathrm{C} 27$ )
b. It costs the firm $\$ 457.60$ to set up the operations (or the fixed cost) without even receiving any order yet
c. Because the p -value is 0.9451 and is larger than 0.05 , thus $\beta_{0}=0$ is confirmed, thus it is not necessary to include the Y intercept term in the regression model
d. The $95 \%$ confidence interval is from -13.1716 to14.0869, it spans zero (or zero is part of the confidence interval), thus $\beta_{0} \neq 0$ is confirmed, thus the $Y$ intercept term should be included in the regression model
3. Which of the following Excel@ function or procedure cannot be used to get the estimates for the regression line ( $b_{0}$ and $b_{1}$ ) or provide predictions:
a. Use Excel@ =SUMPRODUCT(D4:D27,C4:C27) to compute $b_{1}$
b. Click any data point(s) on the scatter plot of the Costs and Orders, select Add Trendline / Display equations \& Display R-Squared value on the chart
c. Use Excel@ =TREND(D4:D27,C4:C27,XValue) to produce predictions
d. Select Data/Data Analysis/Regression with Orders and Costs ranges provided to get regression Summary Output
4. Which one(s) of the following is NOT correct regarding the estimated regression function?
a. The regression line is given by $\hat{Y}=0.4576+0.0161 \mathrm{X}$
b. The regression line is given by $\hat{Y}=0.0161+0.4576 \mathrm{X}$
c. For 3,500 orders, the costs will be around $\$ 56,869.10$ as given by Excel@ $=T R E N D(D 4: D 27, C 4: C 27,3500)$
d. The residual (error) is $\$ 12,219.64$ for 4015 orders as given in the first row of the data set
5. Which one(s) of the following is NOT correct regarding the $R$ Square $\left(R^{2}\right)$ for the data?
a. $84.42 \%$ of the total variations of the data are explained by the regression line.
b. $15.58 \%$ of the total variations of the data are explained by the regression line.
c. It is the ratio of the RSS(Regression Sum of Squares) to TSS (Total Sum of Squares) or RSS/TSS.
d. The multiple $\mathrm{R}=0.9188$ is the square root of the R Square of 0.8442 .
6. What is the percentage of the total variations NOT explained by the regression line?
a. $15.58 \%$
b. $84.42 \%$
c. $91.88 \%$
d. $83.71 \%$
7. The Standard Error of Estimate ( $S_{Y X}$ or $\mathrm{S}_{\mathrm{e}}$ ) to be used to approximate $95 \%$ prediction interval for the costs is:
a. 5.2183
b. 6.5719
c. 0.0015
d. 27.230
8. Which one(s) of the following is NOT correct regarding the relationship between the standard error of estimate $\left(\mathrm{S}_{\mathrm{e}}\right)$ and the standard prediction error $\left(\mathrm{S}_{\mathrm{p}}\right)$ ?
a. $S_{e}$ is always smaller than $S_{p}$
b. $S_{e}$ is always greater than $S_{p}$
c. $S_{e}$ is the RMSE (Root Mean Squared Error) or the square root of MSE
d. $S_{p}$ equals to $S_{e}$ times a value that is greater than one.
9. Which one(s) of the following is NOT correct regarding the $95 \%$ prediction interval of the costs when specifically 4000 orders are received?
a. It is wider than the $95 \%$ prediction interval for the mean costs when 4000 orders are received.
b. It is given by the computed costs $(\hat{Y})$ with the $\mathrm{X}=4000$ orders $(\hat{Y}=0.4576+0.0161 *$ 4000) then plus or minus the margin of prediction error $\left(t S_{p}\right)$
c. It equals to $\hat{Y}_{i} \pm 2 S_{e}$
d. Non of the others is correct.
10. You may notice that the minimum and maximum numbers of orders for the data set are 2921 and 5735 orders respectively. Which one(s) of the following cannot be done regarding the use of the regression line?
a. To predict the costs when 3500 orders are received
b. To predict the costs when 5500 orders are received
c. To predict the costs when 2500 orders are received
d. To predict the costs when 4100 orders are received

|  | A | B | C | D |
| ---: | ---: | ---: | ---: | ---: |
| 3 | Month | Sales | Orders | Cost |
| 4 | 1 | 386 | 4015 | 52.95 |
| 5 | 2 | 446 | 3806 | 71.66 |
| 6 | 3 | 512 | 5309 | 85.58 |
| 7 | 4 | 401 | 4262 | 63.69 |
| 8 | 5 | 457 | 4296 | 72.81 |
| 9 | 6 | 458 | 4097 | 68.44 |
| 10 | 7 | 301 | 3213 | 52.46 |
| 11 | 8 | 484 | 4809 | 70.77 |
| 12 | 9 | 517 | 5237 | 82.03 |
| 13 | 10 | 503 | 4732 | 74.39 |
| 14 | 11 | 535 | 4413 | 70.84 |
| 15 | 12 | 353 | 2921 | 54.08 |
| 16 | 13 | 372 | 3977 | 62.98 |
| 17 | 14 | 328 | 4428 | 72.3 |
| 18 | 15 | 408 | 3964 | 58.99 |
| 19 | 16 | 491 | 4582 | 79.38 |
| 20 | 17 | 527 | 5582 | 94.44 |
| 21 | 18 | 444 | 3450 | 59.74 |
| 22 | 19 | 623 | 5079 | 90.5 |
| 23 | 20 | 596 | 5735 | 93.24 |
| 24 | 21 | 463 | 4269 | 69.33 |
| 25 | 22 | 389 | 3708 | 53.71 |
| 26 | 23 | 547 | 5387 | 89.18 |
| 27 | 24 | 415 | 4161 | 66.8 |
| -1 |  |  |  |  |



| 4 | U | V | W | X | Y | Z | AA |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 30 | SUMMARY OUTPUT |  |  |  |  |  |  |
| 31 |  |  |  |  |  |  |  |
| 32 | Regression Statistics |  |  |  |  |  |  |
| 33 | Multiple R | 0.9188 |  |  |  |  |  |
| 34 | R Square | 0.8442 |  |  |  |  |  |
| 35 | Adjusted R Square | 0.8371 |  |  |  |  |  |
| 36 | Standard Error | 5.2183 |  |  |  |  |  |
| 37 | Observations | 24 |  |  |  |  |  |
| 38 |  |  |  |  |  |  |  |
| 39 | ANOVA |  |  |  |  |  |  |
| 40 |  | $d f$ | SS | MS | $F$ | Significance F |  |
| 41 | Regression | 1 | 3246.062 | 3246.062 | 119.207 | 0.000 |  |
| 42 | Residual | 22 | 599.068 | 27.230 |  |  |  |
| 43 | Total | 23 | 3845.130 |  |  |  |  |
| 44 |  |  |  |  |  |  |  |
| 45 |  | Coefficients | Standard Error | t Stat | $P$-value | Lower 95\% | Upper 95\% |
| 46 | Intercept | 0.4576 | 6.5719 | 0.0696 | 0.9451 | -13.1716 | 14.0869 |
| 47 | Orders | 0.0161 | 0.0015 | 10.9182 | 0.0000 | 0.0131 | 0.0192 |
| 10 |  |  |  |  |  |  |  |

(Berenson, Levine and Krehbiel, $10^{\text {th }}$ Edition, Q. 13.36 on pp. 540-541)

